## An Energy Minimization Approach to the Data Driven Editing of Presegmented Images/Volumes

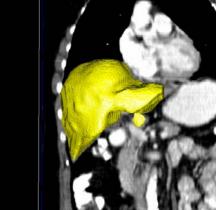
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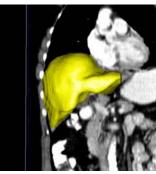
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**Problem – Editing of Automatic Segmentation Results** Want to use natural "seeded" segmentation interface to fix results of incorrect automatic semgentation Incorrect automatic segmentation User interaction







Desired result

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- 1: Independence (no knowledge) of automatic process
- 2: Operation local to interaction site
  - 3: Fast operation
  - 4: 3D modification, despite interaction on a 2D plane
- 5: Data-driven solution

## Formulation

Formulate as a joint energy minimization with presegmentation and interaction

For each pixel *i*:

 $p_i = \begin{cases} 1 & \text{if } v_i \text{ was presegmented as object,} \\ 0 & \text{if } v_j \text{ was presegmented as background.} \end{cases}$ 

Want to solve for  $x_i$ , the probability that pixel *i* belongs to the object, by minimizing:

$$Q(x) = E_{\text{Data/Interaction}} + \gamma E_{\text{Presegmentation}}$$

$$Q(x) = \sum_{e_{ij}} w_{ij} (x_i - x_j)^2 + \gamma \left( \sum_{i} (1 - p_i) x_i + \sum_{i} p_i (1 - x_i) \right)^2$$

Where the weights are determined from the image via:

$$w_{ij} = \exp\left(-\beta(g_i - g_j)^2\right)$$

where  $g_i$  indicates the intensity at voxel *i*. A voxel *i* set as a seed is fixed to  $x_i = 1$  (object) or  $x_i = 0$  (background). Note that it is not necessary to have both object and background seeds.

If x represents real-valued voxel probability: If *x* represents binary voxel membership:

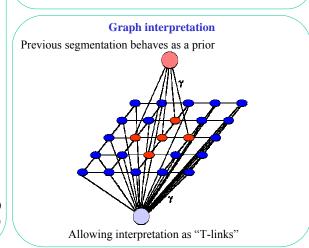
Random walker (linear system solve) Graph cuts (max-flow/min-cut solve)

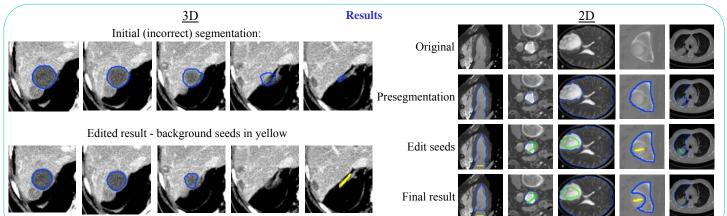
## Locality

In order to enforce locality of interaction, we make  $\gamma$  a function of distance from interaction seeds:

$$\gamma_i = \kappa \exp\left(-\frac{d\left(i,S\right)}{\sigma}\right)$$

where d(i,S) denotes the distance from voxel *i* to any seed (i.e., set S), the parameter  $\sigma$  effects the locality of the interaction and  $\kappa$  indicates the overall strength of the prior segmentation





Green seeds – Object Yellow seeds - Background